## Correlation from Calculus for $A^{\ominus}$ to College Board AP ${ }^{\oplus}$ Calculus $A B$ and $A P^{\circ}$ Calculus BC Framework

| Lesson | Topic(s) | Learning Objective(s) |
| :---: | :--- | :--- |
| Chapter P: Preparation for Calculus |  |  |
| P. 1 | Graphs and Models | Prerequisite topics |
| P. 2 | Linear Models and Rates of Change | Prerequisite topics |
| P. 3 | Functions and Their Graphs | Prerequisite topics |
| P. 4 | Inverse Functions | Prerequisite topics |
| P. 5 | Exponential and Logarithmic Functions | Prerequisite topics |

## Chapter 1: Limits and Their Properties

1.1 A Preview of Calculus
1.2 Finding Limits Graphically and Numerically
1.3 Evaluating Limits Analytically
1.4 Continuity and One-Sided Limits
1.5 Infinite Limits
1.6 Limits at Infinity
1.1
$1.2,1.3,1.4,1.9$
$1.2,1.5,1.6,1.7,1.8,1.9$
$1.3,1.5,1.10,1.11,1.12$, 1.13, 1.16
$1.9,1.10,1.14$
1.9, 1.15

CHA-1.A
LIM-1.A, LIM-1.B, LIM-1.C
LIM-1.B, LIM-1.D, LIM-1.E
LIM-1.C, LIM-1.D, LIM-2.A,
LIM-2.B, LIM-2.C, FUN-1.A
LIM-2.A, LIM-2.D
LIM-2.D

## Chapter 2: Differentiation

2.1 The Derivative and the Tangent Line Problem
2.2 Basic Differentiation Rules and Rates of Change
2.3 Product and Quotient Rules and Higher-Order Derivatives
2.4 The Chain Rule
2.5 Implicit Differentiation
2.6 Derivatives of Inverse Functions
2.7 Related Rates
2.8 Newton's Method

Chapter 3: Applications of Differentiation
3.1 Extrema on an Interval
3.2 Rolle's Theorem and the Mean Value Theorem
3.3 Increasing and Decreasing Functions and the First Derivative Test
3.4 Concavity and the Second Derivative Test
3.5 A Summary of Curve Sketching
3.6 Optimization Problems
3.7 Differentials
5.2, 5.4, 5.5, 5.12
5.1
5.3
5.6, 5.7
5.8, 5.9
5.10, 5.11
4.6

FUN-1.C, FUN-4.A, FUN-4.D
FUN-1.B

FUN-4.A
FUN-4.A
FUN-4.A
FUN-4.B, FUN-4.C
CHA-3.F

| Lesson | Topic(s) | Learning Objective(s) |
| :---: | :---: | :---: |
| Chapter 4: Integration |  |  |
| 4.1 Antiderivatives and Indefinite Integration | 6.7, 6.8, 6.14, 7.1, 7.6, 7.7 | FUN-6.B, FUN-6.C, FUN-7.A, FUN-7.D, FUN-7.E |
| 4.2 Area | 6.1 | CHA-4.A |
| 4.3 Riemann Sums and Definite Integrals | 6.2, 6.3, 6.6, 6.8 | LIM-5.A, LIM-5.B, LIM-5.C, FUN-6.A, FUN-6.C |
| 4.4 The Fundamental Theorem of Calculus | 6.1, 6.4, 6.5, 6.6, 6.7, 8.1, 8.3 | CHA-4.A, CHA-4.B, CHA-4.D, FUN-5.A, FUN-6.A, FUN-6.B |
| 4.5 The Net Change Theorem | 6.1, 8.2, 8.3 | CHA-4.A, CHA-4.C, CHA-4.D, CHA-4.E |
| 4.6 Integration by Substitution | 6.9 | FUN-6.D |
| 4.7 The Natural Logarithmic Function: Integration | 6.10 | FUN-6.D |
| 4.8 Inverse Trigonometric Functions: Integration | 6.10, 6.14 | FUN-6.D |
| Chapter 5: Differential Equations |  |  |
| 5.1 Slope Fields and Euler's Method | 7.1, 7.2, 7.3, 7.4, 7.5, 7.7 | FUN-7.A, FUN-7.B, FUN-7.C, FUN-7.E |
| 5.2 Growth and Decay | 7.6, 7.7, 7.8 | FUN-7.D, FUN-7.E, FUN-7.F, FUN-7.G |
| 5.3 Separation of Variables | 7.6, 7.7 | FUN-7.D, FUN-7.E |
| 5.4 The Logistic Equation | 7.9 | FUN-7.H |
| Chapter 6: Applications of Integration |  |  |
| 6.1 Area of a Region Between Two Curves | 8.4, 8.5, 8.6 | CHA-5.A |
| 6.2 Volume: The Disk and Washer Methods | 8.7, 8.8, 8.9, 8.10, 8.11, 8.12 | CHA-5.B, CHA-5.C |
| 6.3 Volume: The Shell Method |  |  |
| 6.4 Arc Length and Surfaces of Revolution | 8.13 | CHA-6.A |
| Chapter 7: Integration Techniques, L'Hôpital's Rule, and Improper Integrals |  |  |
| 7.1 Basic Integration Rules | 6.9, 6.10, 6.14 | FUN-6.D |
| 7.2 Integration by Parts | 6.11, 6.14 | FUN-6.E |
| 7.3 Trigonometric Integrals | 6.14 |  |
| 7.4 Trigonometric Substitution | 6.14 |  |
| 7.5 Partial Fractions | 6.12, 6.14 | FUN-6.F |
| 7.6 Integration by Tables and Other Integration Techniques | 6.14 |  |
| 7.7 Indeterminate Forms and L'Hôpital's Rule | 4.7 | LIM-4.A |
| 7.8 Improper Integrals | 6.13 | LIM-6.A |


| Lesson | Topic(s) | Learning Objective(s) |
| :--- | :--- | :--- |
| Chapter 8: Infinite Series |  |  |
| 8.1 | Sequences | $10.1,10.2,10.3$ |
| 8.2 | Series and Convergence | $10.4,10.5$ |
| 8.3 | The Integral Test and $p$-Series | 10.6 |
| 8.4 | Comparisons of Series | $10.7,10.9,10.10$ |
| 8.5 | Alternating Series | 10.8 |
| 8.6 | The Ratio and Root Tests | LIM-7.A.A |
| 8.7 | Taylor Polynomials and Approximations | $10.11,10.12$ |
| 8.8 | Power Series | LIM-7.A |
| 8.9 | Representation of Functions | LIM-7.A LIM-7.B |
|  | by Power Series | LIM-8.A, LIM-8.B, LIM-8.C |
| 8.10 | Taylor and Maclaurin Series | $10.13,10.14,10.15$ |
|  |  | LIM-8.D |
| Chapter 9: Parametric Equations, Polar Coordinates, and Vectors |  |  |
| 9.1 | Conics and Calculus |  |
| 9.2 | Plane Curves and Parametric Equations |  |
| 9.3 | Parametric Equations and Calculus | $9.1,9.2,9.3$ |
| 9.4 | Polar Coordinates and Polar Graphs | 9.7 |
| 9.5 | Area and Arc Length in Polar Coordinates | $9.8,9.9$ |
| 9.6 | Vectors in the Plane |  |
| 9.7 | Vector-Valued Functions |  |
| 9.8 | Velocity and Acceleration | CHA-3.G, CHA-6.B |

# Correlation from College Board AP ${ }^{\ominus}$ Calculus AB and AP ${ }^{\oplus}$ Calculus BC Framework to Calculus for AP ${ }^{\circ}$ 

## Course: $\mathrm{AP}^{\circledR}$ Calculus AB and BC

## Unit 1: Limits and Continuity

Suggested Length: AB ~22-23 class periods $B C \sim 13-14$ class periods

AP Exam Weighting: AB 10-12\%<br>BC 4-7\%

Big Ideas: Change (CHA); Limits (LIM); Analysis of Functions (FUN)

| Topic | Enduring Understanding and Learning Objective | Essential Knowledge | Text Section(s) \& Page Number(s) |
| :---: | :---: | :---: | :---: |
| 1.1: Introducing Calculus: Can Change Occur at an Instant? | CHA-1: Calculus allows us to generalize knowledge about motion to diverse problems involving change. <br> CHA-1.A: Interpret the rate of change at an instant in terms of average rates of change over intervals containing that instant. | CHA-1.A. 1 | 1.1, pp. 58-59 |
|  |  | CHA-1.A. 2 | 1.1, pp. 58-59 |
|  |  | CHA-1.A. 3 | 1.1, pp. 58-59 |
| 1.2: Defining <br> Limits and Using <br> Limit Notation | LIM-1: Reasoning with definitions, theorems, and properties can be used to justify claims about limits. <br> LIM-1.A: Represent limits analytically using correct notation. | LIM-1.A. 1 | 1.2, p. 65 |
|  | LIM-1: Reasoning with definitions, theorems, and properties can be used to justify claims about limits. <br> LIM-1.B: Interpret limits expressed in analytic notation. | LIM-1.B. 1 | $\begin{aligned} & \text { 1.2, pp. 65-71 } \\ & \text { 1.3, pp. 76-83 } \end{aligned}$ |
| 1.3: Estimating Limit Values from Graphs | LIM-1: Reasoning with definitions, theorems, and properties can be used to justify claims about limits. <br> LIM-1.C: Estimate limits of functions. | LIM-1.C. 1 | 1.4, pp. 89-91 |
|  |  | LIM-1.C. 2 | 1.2, p. 66 |
|  |  | LIM-1.C. 3 | 1.2, p. 68 |
|  |  | LIM-1.C. 4 | 1.2, pp. 67-68 |
| 1.4: Estimating Limit Values from Tables | LIM-1: Reasoning with definitions, theorems, and properties can be used to justify claims about limits. <br> LIM-1.C: Estimate limits of functions. | LIM-1.C. 5 | 1.2, p. 66 |
| 1.5: Determining <br> Limits Using <br> Algebraic <br> Properties of Limits | LIM-1: Reasoning with definitions, theorems, and properties can be used to justify claims about limits. <br> LIM-1.D: Determine the limits of functions using limit theorems. | LIM-1.D. 1 | 1.4, pp. 89-91 |
|  |  | LIM-1.D. 2 | 1.3, pp. 76-78 |
| 1.6: Determining <br> Limits Using <br> Algebraic <br> Manipulation | LIM-1: Reasoning with definitions, theorems, and properties can be used to justify claims about limits. <br> LIM-1.E: Determine the limits of functions using equivalent expressions for the function or the squeeze theorem. | LIM-1.E. 1 | 1.3, pp. 79-83 |


| Topic | Enduring Understanding and Learning Objective | Essential Knowledge | Text Section(s) \& Page Number(s) |
| :---: | :---: | :---: | :---: |
| 1.7: Selecting Procedures for Determining Limits |  |  | 1.3, p. 79 |
| 1.8: Determining Limits Using the Squeeze Theorem | LIM-1: Reasoning with definitions, theorems, and properties can be used to justify claims about limits. <br> LIM-1.E: Determine the limits of functions using equivalent expressions for the function or the squeeze theorem. | LIM-1.E. 2 | 1.3, pp. 82-83 |
| 1.9: Connecting Multiple Representations of Limits |  |  | 1.2, p. 66, Example 1 1.3, p. 83, Example 9 1.5, p. 101, Example 1 1.6, p. 110, Example 2 |
| 1.10: Exploring Types of Discontinuities | LIM-2: Reasoning with definitions, theorems, and properties can be used to justify claims about continuity. <br> LIM-2.A: Justify conclusions about continuity at a point using the definition. | LIM-2.A. 1 | $\begin{aligned} & 1.4, \text { p. } 88 \\ & 1.5 \text {, pp. } 102-104 \end{aligned}$ |
| 1.11: Defining Continuity at a Point | LIM-2: Reasoning with definitions, theorems, and properties can be used to justify claims about continuity. <br> LIM-2.A: Justify conclusions about continuity at a point using the definition. | LIM-2.A. 2 | 1.4, pp. 87-88 |
| 1.12: Confirming Continuity over an Interval | LIM-2: Reasoning with definitions, theorems, and properties can be used to justify claims about continuity. <br> LIM-2.B: Determine intervals over which a function is continuous. | LIM-2.B. 1 | 1.4, pp. 87-95 |
|  |  | LIM-2.B. 2 | 1.4, p. 92 |
| 1.13: Removing Discontinuities | LIM-2: Reasoning with definitions, theorems, and properties can be used to justify claims about continuity. <br> LIM-2.C: Determine values of $x$ or solve for parameters that make discontinuous functions continuous, if possible. | LIM-2.C. 1 | 1.4, p. 88 |
|  |  | LIM-2.C. 2 | 1.4, p. 88 |
| 1.14: Connecting Infinite Limits and Vertical Asymptotes | LIM-2: Reasoning with definitions, theorems, and properties can be used to justify claims about continuity. <br> LIM-2.D: Interpret the behavior of functions using limits involving infinity. | LIM-2.D. 1 | 1.5, pp. 100-104 |
|  |  | LIM-2.D. 2 | 1.5, pp. 100-104 |
| 1.15: Connecting Limits at Infinity and Horizontal Asymptotes | LIM-2: Reasoning with definitions, theorems, and properties can be used to justify claims about continuity. <br> LIM-2.D: Interpret the behavior of functions using limits involving infinity. | LIM-2.D. 3 | 1.6, pp. 108-114 |
|  |  | LIM-2.D. 4 | 1.6, pp. 108-114 |
|  |  | LIM-2.D. 5 | 1.6, pp. 108-114 |
| 1.16: Working with the Intermediate Value Theorem (IVT) | FUN-1: Existence theorems allow us to draw conclusions about a function's behavior on an interval without precisely locating that behavior. <br> FUN-1.A: Explain the behavior of a function on an interval using the Intermediate Value Theorem. | FUN-1.A. 1 | 1.4, pp. 94-95 |

# Course: $\mathrm{AP}^{\circledR}$ Calculus AB and BC <br> Unit 2: Differentiation: Definition and Fundamental Properties <br> Suggested Length: AB $\sim 13-14$ class periods AP Exam Weighting: AB 10-12\% $B C \sim 9-10$ class periods BC 4-7\% 

Big Ideas: Change (CHA); Limits (LIM); Analysis of Functions (FUN)

| Topic | Enduring Understanding and Learning Objective | Essential Knowledge | Text Section(s) \& Page Number(s) |
| :---: | :---: | :---: | :---: |
| 2.1: Defining Average and Instantaneous Rates of Change at a Point | CHA-2: Derivatives allow us to determine rates of change at an instant by applying limits to knowledge about rates of change over intervals. <br> CHA-2.A: Determine average rates of change using difference quotients. | CHA-2.A. 1 | $\begin{aligned} & \text { 2.1, p. } 125 \\ & \text { 2.2, pp. 142-143 } \end{aligned}$ |
|  | CHA-2: Derivatives allow us to determine rates of change at an instant by applying limits to knowledge about rates of change over intervals. <br> CHA-2.B: Represent the derivative of a function as the limit of a difference quotient. | CHA-2.B. 1 | $\begin{aligned} & \text { 2.1, p. } 127 \\ & \text { 2.2, pp. 142-143 } \end{aligned}$ |
| 2.2: Defining the Derivative of a Function and Using Derivative Notation | CHA-2: Derivatives allow us to determine rates of change at an instant by applying limits to knowledge about rates of change over intervals. <br> CHA-2.B: Represent the derivative of a function as the limit of a difference quotient. | CHA-2.B. 2 | 2.1, p. 127 |
|  |  | CHA-2.B. 3 | 2.1, p. 127 |
|  |  | CHA-2.B. 4 | 2.1, pp. 127-128 |
|  | CHA-2: Derivatives allow us to determine rates of change at an instant by applying limits to knowledge about rates of change over intervals. <br> CHA-2.C: Determine the equation of a line tangent to a curve at a given point. | CHA-2.C. 1 | 2.1, pp. 124-128 |
| 2.3: Estimating <br> Derivatives of a <br> Function at a <br> Point | CHA-2: Derivatives allow us to determine rates of change at an instant by applying limits to knowledge about rates of change over intervals. <br> CHA-2.D: Estimate derivatives. | CHA-2.D. 1 | 2.1, p. 132, <br> Exercises 1-2 <br> AP Exam Practice <br> Questions for <br> Chapter 2, p. 209, <br> Exercise 8 |
|  |  | CHA-2.D. 2 | 2.1, p. 130 |
| 2.4: Connecting Differentiability and Continuity: Determining When Derivatives Do and Do Not Exist | FUN-2: Recognizing that a function's derivative may also be a function allows us to develop knowledge about the related behaviors of both. <br> FUN-2.A: Explain the relationship between differentiability and continuity. | FUN-2.A. 1 | 2.1, pp. 129-130 |
|  |  | FUN-2.A. 2 | 2.1, pp. 129-130 |
| 2.5: Applying the Power Rule | FUN-3: Recognizing opportunities to apply derivative rules can simplify differentiation. <br> FUN-3.A: Calculate derivatives of familiar functions. | FUN-3.A. 1 | 2.2, pp. 136-137 |
| 2.6: Derivative Rules: Constant, Sum, Difference, and Constant Multiple | FUN-3: Recognizing opportunities to apply derivative rules can simplify differentiation. <br> FUN-3.A: Calculate derivatives of familiar functions. | FUN-3.A. 2 | 2.2, pp. 135, 138-139 |
|  |  | FUN-3.A. 3 | 2.2, p. 139 |


| Topic | Enduring Understanding and Learning Objective | Essential Knowledge | Text Section(s) \& Page Number(s) |
| :---: | :---: | :---: | :---: |
| 2.7: Derivatives of $\cos x, \sin x, e^{x}$, and $\ln x$ | FUN-3: Recognizing opportunities to apply derivative rules can simplify differentiation. <br> FUN-3.A: Calculate derivatives of familiar functions. | FUN-3.A. 4 | 2.2, pp. 140-141 2.4, pp. 165-168 |
|  | LIM-3: Reasoning with definitions, theorems, and properties can be used to determine a limit. <br> LIM-3.A: Interpret a limit as a definition of a derivative. | LIM-3.A. 1 | 2.1, p. 127 |
| 2.8: The Product Rule | FUN-3: Recognizing opportunities to apply derivative rules can simplify differentiation. <br> FUN-3.B: Calculate derivatives of products and quotients of differentiable functions. | FUN-3.B. 1 | 2.3, pp. 148-149 |
| 2.9: The Quotient Rule | FUN-3: Recognizing opportunities to apply derivative rules can simplify differentiation. <br> FUN-3.B: Calculate derivatives of products and quotients of differentiable functions. | FUN-3.B. 2 | 2.3, pp. 150-152 |
| 2.10: Finding the Derivatives of Tangent, Cotangent, Secant, and/or Cosecant Functions | FUN-3: Recognizing opportunities to apply derivative rules can simplify differentiation. <br> FUN-3.B: Calculate derivatives of products and quotients of differentiable functions. | FUN-3.B. 3 | 2.3, pp. 152-153 |

Course: $\mathrm{AP}^{\circledR}$ Calculus AB and BC
Unit 3: Differentiation: Composite, Implicit, and Inverse Functions

Suggested Length: | $A B$ | $10-11$ class periods |
| :--- | :--- |
| $B C \sim 8-9$ | class periods |$\quad$ AP Exam Weighting: AB 9-13\%

BC $4-7 \%$

Big Ideas: Analysis of Functions (FUN)

| Topic | Enduring Understanding and Learning Objective | Essential <br> Knowledge |  <br> Page Number(s) |
| :--- | :--- | :--- | :--- |
| 3.1: The Chain <br> Rule | FUN-3: Recognizing opportunities to apply derivative rules can simplify <br> differentiation. <br> FUN-3.C: Calculate derivatives of compositions of differentiable <br> functions. | FUN-3.C.1 | 2.4, pp. 159-168 |


| Topic | Enduring Understanding and Learning Objective | Essential <br> Knowledge |  <br> Page Number(s) |
| :--- | :--- | :--- | :--- |
| 3.4: <br> Differentiating <br> Inverse <br> Trigonometric <br> Functions | FUN-3: Recognizing opportunities to apply derivative rules can simplify <br> differentiation. <br> FUN-3.E: Calculate derivatives of inverse and inverse trigonometric <br> functions. | FUN-3.E.2 | 2.6, pp. 184-186 |
| 3.5: Selecting <br> Procedures for <br> Calculating <br> Derivatives |  | 2.4, p. 168 |  |
| 3.6: Calculating <br> Higher-Order <br> Derivatives | FUN-3: Recognizing opportunities to apply derivative rules can simplify <br> differentiation. | FUN-3.F.1 | 2.3, p. 153 |
|  | FUN-3.F: Determine higher-order derivatives of a function. | FUN-3.F.2 | 2.3, p. 153 |

Course: $\mathrm{AP}^{\circledR}$ Calculus AB and BC
Unit 4: Contextual Applications of Differentiation

$$
\begin{array}{rrl}
\text { Suggested Length: } & \mathrm{AB} \sim 10-11 \text { class periods } & \text { AP Exam Weighting: } \begin{array}{l}
\text { AB } 10-15 \% \\
\\
\mathrm{BC} \sim 6-7 \text { class periods }
\end{array} \\
\text { BC } 6-9 \%
\end{array}
$$

Big Ideas: Change (CHA); Limits (LIM)

| Topic | Enduring Understanding and Learning Objective | Essential Knowledge | Text Section(s) \& Page Number(s) |
| :---: | :---: | :---: | :---: |
| 4.1: Interpreting the Meaning of the Derivative in Context | CHA-3: Derivatives allow us to solve real-world problems involving rates of change. <br> CHA-3.A: Interpret the meaning of a derivative in context. | CHA-3.A. 1 | 2.1, p. 127 |
|  |  | CHA-3.A. 2 | 2.2, pp. 142-143 |
|  |  | CHA-3.A. 3 | 2.2, pp. 142-143 |
| 4.2: StraightLine Motion: Connecting Position, Velocity, and Acceleration | CHA-3: Derivatives allow us to solve real-world problems involving rates of change. <br> CHA-3.B: Calculate rates of change in applied contexts. | CHA-3.B. 1 | $\begin{aligned} & 2.2 \text {, pp. } 142-143 \\ & 2.3 \text {, p. } 154 \\ & 2.7 \text {, pp. } 193-194 \end{aligned}$ |
| 4.3: Rates of Change in Applied Contexts Other Than Motion | CHA-3: Derivatives allow us to solve real-world problems involving rates of change. <br> CHA-3.C: Interpret rates of change in applied contexts. | CHA-3.C. 1 | 2.7, pp. 191-192 |
| 4.4: Introduction to Related Rates | CHA-3: Derivatives allow us to solve real-world problems involving rates of change. <br> CHA-3.D: Calculate related rates in applied contexts. | CHA-3.D. 1 | 2.7, pp. 190-194 |
|  |  | CHA-3.D. 2 | 2.7, pp. 190-194 |
| 4.5: Solving Related Rates Problems | CHA-3: Derivatives allow us to solve real-world problems involving rates of change. <br> CHA-3.E: Interpret related rates in applied contexts. | CHA-3.E. 1 | 2.7, pp. 190-194 |


| Topic | Enduring Understanding and Learning Objective | Essential <br> Knowledge |  <br> Page Number(s) |
| :--- | :--- | :--- | :--- |
| 4.6: <br> Approximating <br> Values of a <br> Function Using <br> Local Linearity <br> and Linearization | CHA-3: Derivatives allow us to solve real-world problems involving <br> rates of change. <br> CHA-3.F: Approximate a value on a curve using the equation of a <br> tangent line. | CHA-3.F.1 | 3.7, pp. 267-271 |
| 4.7: Using <br> L'Hospital's Rule <br> for Determining <br> Limits of <br> Indeterminate <br> Forms | LIM-4: L'Hospital's rule allows us to determine the limits of some <br> indeterminate forms. <br> LIM-4.A: Determine limits of functions that result in indeterminate <br> forms. | CHA-3.F.2 | 3.7, pp. 267-271 |

Course: $\mathrm{AP}^{\circledR}$ Calculus AB and BC
Unit 5: Analytical Applications of Differentiation
Suggested Length: AB ~15-16 class periods AP Exam Weighting: AB 15-18\% BC $\sim 10-11$ class periods BC 8-11\%

Big Ideas: Analysis of Functions (FUN)

| Topic | Enduring Understanding and Learning Objective | Essential <br> Knowledge |  <br> Page Number(s) |
| :--- | :--- | :--- | :--- |
| 5.1: Using the <br> Mean Value <br> Theorem | FUN-1: Existence theorems allow us to draw conclusions about a <br> function's behavior on an interval without precisely locating that behavior. <br> FUN-1.B: Justify conclusions about functions by applying the <br> Mean Value Theorem over an interval. | FUN-1.B.1 | 3.2, pp. 222-223 |


| Topic | Enduring Understanding and Learning Objective | Essential <br> Knowledge |  <br> Page Number(s) |
| :--- | :--- | :--- | :--- |
| 5.6: Determining <br> Concavity of <br> Functions over <br> Their Domains | FUN-4: A function's derivative can be used to understand some <br> behaviors of the function. <br> FUN-4.A: Justify conclusions about the behavior of a function based <br> on the behavior of its derivatives. | FUN-4.A.4 | 3.4, p. 237 |
|  |  | FUN-4.A.6 | 3.4, pp. 239-240 |
| 5.7: Using the <br> Second Derivative <br> Test to Find <br> Extrema | FUN-4: A function's derivative can be used to understand some <br> behaviors of the function. <br> FUN-4.A: Justify conclusions about the behavior of a function based <br> on the behavior of its derivatives. | FUN-4.A.7 | 3.4, p. 241 |
| 5.8: Sketching <br> Graphs of | FUN-4: A function's derivative can be used to understand some <br> behaviors of the function. | FUN-4.A.9 | 3.5, pp. 245-252 |
| Functions and <br> Their Derivatives | FUN-4.A: Justify conclusions about the behavior of a function based <br> on the behavior of its derivatives. | FUN-4.A.10 | 3.5, pp. 245-252 |
| 5.9: Connecting a <br> Function, Its First | FUN-4: A function's derivative can be used to understand some <br> behaviors of the function. |  | FUn |

Course: $\mathrm{AP}^{\circledR}$ Calculus AB and BC
Unit 6: Integration and Accumulation of Change
Suggested Length: AB $\sim 18-20$ class periods AP Exam Weighting: AB 17-20\% BC ~15-16 class periods BC 17-20\%
Big Ideas: Change (CHA); Limits (LIM); Analysis of Functions (FUN)

| Topic | Enduring Understanding and Learning Objective | Essential Knowledge | Text Section(s) \& Page Number(s) |
| :---: | :---: | :---: | :---: |
| 6.1: Exploring Accumulations of Change | CHA-4: Definite integrals allow us to solve problems involving the accumulation of change over an interval. <br> CHA-4.A: Interpret the meaning of areas associated with the graph of a rate of change in context. | CHA-4.A. 1 | $\begin{aligned} & 4.4, \text { p. } 323 \\ & 4.5 \text {, p. } 330 \end{aligned}$ |
|  |  | CHA-4.A. 2 | 4.2, pp. 292-293 |
|  |  | CHA-4.A. 3 | 4.5, p. 331 |
|  |  | CHA-4.A.4 | 4.5, p. 330 |
| 6.2: Approximating Areas with Riemann Sums | LIM-5: Definite integrals can be approximated using geometric and numerical methods. <br> LIM-5.A: Approximate a definite integral using geometric and numerical methods. | LIM-5.A. 1 | 4.3, pp. 304-311 |
|  |  | LIM-5.A. 2 | $\begin{aligned} & \text { 4.3, pp. 302-305, } \\ & 309-311 \end{aligned}$ |
|  |  | LIM-5.A. 3 | 4.3, pp. 309-310 |
|  |  | LIM-5.A. 4 | 4.3, pp. 309-310 |
| 6.3: Riemann Sums, Summation Notation, and Definite Integral Notation | LIM-5: Definite integrals can be approximated using geometric and numerical methods. <br> LIM-5.B: Interpret the limiting case of the Riemann sum as a definite integral. | LIM-5.B. 1 | 4.3, pp. 304-305 |
|  |  | LIM-5.B.2 | 4.3, pp. 302-303 |
|  | LIM-5: Definite integrals can be approximated using geometric and numerical methods. <br> LIM-5.C: Represent the limiting case of the Riemann sum as a definite integral. | LIM-5.C. 1 | 4.3, p. 304 |
|  |  | LIM-5.C. 2 | 4.3, p. 304 |
| 6.4: The <br> Fundamental <br> Theorem of Calculus and Accumulation Functions | FUN-5: The Fundamental Theorem of Calculus connects differentiation and integration. <br> FUN-5.A: Represent accumulation functions using definite integrals. | FUN-5.A. 1 | 4.4, pp. 323-325 |
|  |  | FUN-5.A. 2 | 4.4, pp. 324-325 |
| 6.5: Interpreting the Behavior of Accumulation Functions Involving Area | FUN-5: The Fundamental Theorem of Calculus connects differentiation and integration. <br> FUN-5.A: Represent accumulation functions using definite integrals. | FUN-5.A. 3 | 4.4, pp. 323-325 |
| 6.6: Applying Properties of Definite Integrals | FUN-6: Recognizing opportunities to apply knowledge of geometry and mathematical rules can simplify integration. <br> FUN-6.A: Calculate a definite integral using areas and properties of definite integrals. | FUN-6.A. 1 | 4.4, pp. 320-321 |
|  |  | FUN-6.A. 2 | 4.3, pp. 307-308 |
|  |  | FUN-6.A. 3 | 4.3, p. 308 |


| Topic | Enduring Understanding and Learning Objective | Essential Knowledge | Text Section(s) \& Page Number(s) |
| :---: | :---: | :---: | :---: |
| 6.7: The <br> Fundamental <br> Theorem of Calculus and Definite Integrals | FUN-6: Recognizing opportunities to apply knowledge of geometry and mathematical rules can simplify integration. <br> FUN-6.B: Evaluate definite integrals analytically using the Fundamental Theorem of Calculus. | FUN-6.B. 1 | 4.1, pp. 280-281 |
|  |  | FUN-6.B. 2 | 4.4, pp. 324-325 |
|  |  | FUN-6.B. 3 | 4.4, pp. 317-319 |
| 6.8: Finding Antiderivatives and Indefinite Integrals: Basic Rules and Notation | FUN-6: Recognizing opportunities to apply knowledge of geometry and mathematical rules can simplify integration. <br> FUN-6.C: Determine antiderivatives of functions and indefinite integrals, using knowledge of derivatives. | FUN-6.C. 1 | 4.1, pp. 280-281 |
|  |  | FUN-6.C. 2 | 4.1, pp. 282-284 |
|  |  | FUN-6.C. 3 | 4.3, p. 309 |
| 6.9: Integrating Using Substitution | FUN-6: Recognizing opportunities to apply knowledge of geometry and mathematical rules can simplify integration. <br> FUN-6.D: For integrands requiring substitution or rearrangements into equivalent forms: <br> (a) Determine indefinite integrals. <br> (b) Evaluate definite integrals. | FUN-6.D. 1 | $\begin{aligned} & 4.6 \text {, pp. } 337-342 \\ & 7.1, \text { pp. } 456-459 \end{aligned}$ |
|  |  | FUN-6.D. 2 | 4.6, pp. 340-342 |
| 6.10: Integrating Functions Using Long Division and Completing the Square | FUN-6: Recognizing opportunities to apply knowledge of geometry and mathematical rules can simplify integration. <br> FUN-6.D: For integrands requiring substitution or rearrangements into equivalent forms: <br> (a) Determine indefinite integrals. <br> (b) Evaluate definite integrals. | FUN-6.D. 3 | $\begin{aligned} & \text { 4.7, p. } 349 \\ & \text { 4.8, p. } 358 \\ & \text { 7.1, pp. } 456,459 \end{aligned}$ |
| 6.11: Integrating Using Integration by Parts BC ONLY | FUN-6: Recognizing opportunities to apply knowledge of geometry and mathematical rules can simplify integration. <br> FUN-6.E: For integrands requiring integration by parts: <br> (a) Determine indefinite integrals. BC ONLY <br> (b) Evaluate definite integrals. BC ONLY | FUN-6.E. 1 | 7.2, pp. 463-468 |
| 6.12: Integrating <br> Using Linear <br> Partial Fractions <br> BC ONLY | FUN-6: Recognizing opportunities to apply knowledge of geometry and mathematical rules can simplify integration. <br> FUN-6.F: For integrands requiring integration by linear partial fractions: <br> (a) Determine indefinite integrals. BC ONLY <br> (b) Evaluate definite integrals. BC ONLY | FUN-6.F. 1 | 7.5, pp. 491-497 |
| 6.13: Evaluating Improper Integrals BC ONLY | LIM-6: The use of limits allows us to show that the areas of unbounded regions may be finite. <br> LIM-6.A: Evaluate an improper integral or determine that the integral diverges. BC ONLY | LIM-6.A. 1 | 7.8, p. 517 |
|  |  | LIM-6.A. 2 | 7.8, pp. 517-523 |
| 6.14: Selecting Techniques for Antidifferentiation |  |  | $\begin{aligned} & \text { 4.1, p. } 282 \\ & \text { 4.8, p. } 359 \\ & 7.1 \text {, p. } 459 \\ & 7.2-7.6 \text {, pp. } 463-505 \end{aligned}$ |

Course: $\mathrm{AP}^{\circledR}$ Calculus AB and BC
Unit 7: Differential Equations
Suggested Length: AB $\sim 8-9$ class periods $\mathrm{BC} \sim 9-10$ class periods

AP Exam Weighting: AB 6-12\%
BC 6-9\%

Big Ideas: Analysis of Functions (FUN)

| Topic | Enduring Understanding and Learning Objective | Essential <br> Knowledge |  <br> Page Number(s) |
| :--- | :--- | :--- | :--- |
| 7.1: Modeling <br> Situations with <br> Differential <br> Equations | FUN-7: Solving differential equations allows us to determine <br> functions and develop models. <br> FUN-7.A: Interpret verbal statements of problems as differential <br> equations involving a derivative expression. | FUN-7.A.1 | 4.1, p. 281 <br> 5.1, p. 370 |
| 7.2: Verifying <br> Solutions for <br> Differential <br> Equations | FUN-7: Solving differential equations allows us to determine functions <br> and develop models. <br> FUN-7.B: Verify solutions to differential equations. | FUN-7.B.1 | 5.1, pp. 370-371 |
| 7.3: Sketching <br> Slope Fields | FUN-7: Solving differential equations allows us to determine functions <br> and develop models. | FUN-7.C.1 | FUN-7.B.2 | 5.1, pp. 372-373 | 5.1, pp. 370-371 |
| :--- |


| Topic | Enduring Understanding and Learning Objective | Essential <br> Knowledge |  <br> Page Number(s) |
| :--- | :--- | :--- | :--- |
|  | FUN-7: Solving differential equations allows us to determine <br> functions and develop models. <br> FUN-7.F: Interpret the meaning of a differential equation and its <br> variables in context. | FUN-7.F.1 | 5.2, pp. 380-383 |
|  | FUN-7: Solving differential equations allows us to determine functions <br> and develop models. <br> FUN-7.G: Determine general and particular solutions for problems <br> involving differential equations in context. | FUN-7.F.2 | 5.2, p. 380 |
| 7.9: Logistic <br> Models with <br> Differential <br> Equations <br> BC ONLY | FUN-7: Solving differential equations allows us to determine functions <br> and develop models. | FUN-7.H.1 | 5.5 5.2, pp. 380-383 |
| FUN-7.H: Interpret the meaning of the logistic growth model in |  |  |  |
| Context. BC ONLY |  |  |  |

## Course: $\mathrm{AP}^{\circledR}$ Calculus AB and BC

Unit 8: Applications of Integration
Suggested Length: AB ~19-20 class periods

> AP Exam Weighting: AB $10-15 \%$
> BC 6-9\%

Big Ideas: Change (CHA)

| Topic | Enduring Understanding and Learning Objective | Essential <br> Knowledge |  <br> Page Number(s) |
| :--- | :--- | :--- | :--- |
| 8.1: Finding the <br> Average Value of <br> a Function on an <br> Interval | CHA-4: Definite integrals allow us to solve problems involving the <br> accumulation of change over an interval. <br> CHA-4.B: Determine the average value of a function using definite <br> integrals. | CHA-4.B.1 | 4.4, pp. 321-322 |


| Topic | Enduring Understanding and Learning Objective | Essential Knowledge | Text Section(s) \& Page Number(s) |
| :---: | :---: | :---: | :---: |
| 8.4: Finding the Area Between Curves Expressed as Functions of $x$ | CHA-5: Definite integrals allow us to solve problems involving the accumulation of change in area or volume over an interval. <br> CHA-5.A: Calculate areas in the plane using the definite integral. | CHA-5.A. 1 | 6.1, pp. 410-415 |
| 8.5: Finding the Area Between Curves Expressed as Functions of $y$ | CHA-5: Definite integrals allow us to solve problems involving the accumulation of change in area or volume over an interval. <br> CHA-5.A: Calculate areas in the plane using the definite integral. | CHA-5.A. 2 | 6.1, p. 414 |
| 8.6: Finding the Area Between Curves That Intersect at More Than Two Points | CHA-5: Definite integrals allow us to solve problems involving the accumulation of change in area or volume over an interval. <br> CHA-5.A: Calculate areas in the plane using the definite integral. | CHA-5.A. 3 | 6.1, pp. 413-414 |
| 8.7: Volumes with Cross Sections: <br> Squares and Rectangles | CHA-5: Definite integrals allow us to solve problems involving the accumulation of change in area or volume over an interval. <br> CHA-5.B: Calculate volumes of solids with known cross sections using definite integrals. | CHA-5.B. 1 | 6.2, pp. 425-426 |
| 8.8: Volumes with Cross Sections: Triangles and Semicircles | CHA-5: Definite integrals allow us to solve problems involving the accumulation of change in area or volume over an interval. <br> CHA-5.B: Calculate volumes of solids with known cross sections using definite integrals. | CHA-5.B. 2 | 6.2, pp. 425-426 |
|  |  | CHA-5.B. 3 | 6.2, pp. 425-426 |
| 8.9: Volume with Disc Method: Revolving Around the $x$ - or $y$-Axis | CHA-5: Definite integrals allow us to solve problems involving the accumulation of change in area or volume over an interval. <br> CHA-5.C: Calculate volumes of solids of revolution using definite integrals. | CHA-5.C. 1 | 6.2, pp. 420-422 |
| 8.10: Volume with Disc Method: <br> Revolving Around Other Axes | CHA-5: Definite integrals allow us to solve problems involving the accumulation of change in area or volume over an interval. <br> CHA-5.C: Calculate volumes of solids of revolution using definite integrals. | CHA-5.C. 2 | 6.2, pp. 420-422 |
| 8.11: Volume with Washer Method: Revolving Around the $x$ - or $y$-Axis | CHA-5: Definite integrals allow us to solve problems involving the accumulation of change in area or volume over an interval. <br> CHA-5.C: Calculate volumes of solids of revolution using definite integrals. | CHA-5.C. 3 | 6.2, pp. 423-425 |
| 8.12: Volume with Washer Method: Revolving Around Other Axes | CHA-5: Definite integrals allow us to solve problems involving the accumulation of change in area or volume over an interval. <br> CHA-5.C: Calculate volumes of solids of revolution using definite integrals. | CHA-5.C. 4 | 6.2, pp. 423-425 |
| 8.13: The Arc <br> Length of a <br> Smooth, Planar <br> Curve and <br> Distance Traveled <br> BC ONLY | CHA-6: Definite integrals allow us to solve problems involving the accumulation of change in length over an interval. <br> CHA-6.A: Determine the length of a curve in the plane defined by a function, using a definite integral. BC ONLY | CHA-6.A. 1 | 6.4, pp. 440-443 |

## Course: AP ${ }^{\circledR}$ Calculus BC Only

Unit 9: Parametric Equations, Polar Coordinates, and Vector-Valued Functions
Suggested Length: AB Not Applicable AP Exam Weighting: AB Not Applicable $B C \sim 10-11$ class periods

BC 11-12\%
Big Ideas: Change (CHA); Analysis of Functions (FUN)

| Topic | Enduring Understanding and Learning Objective | Essential Knowledge | Text Section(s) \& Page Number(s) |
| :---: | :---: | :---: | :---: |
| 9.1: Defining and Differentiating <br> Parametric <br> Equations <br> BC ONLY | CHA-3: Derivatives allow us to solve real-world problems involving rates of change. <br> CHA-3.G: Calculate derivatives of parametric functions. BC ONLY | CHA-3.G. 1 | 9.3, pp. 655-658 |
|  |  | CHA-3.G. 2 | 9.3, pp. 655-658 |
| 9.2: Second <br> Derivatives <br> of Parametric <br> Equations <br> BC ONLY | CHA-3: Derivatives allow us to solve real-world problems involving rates of change. <br> CHA-3.G: Calculate derivatives of parametric functions. BC ONLY | CHA-3.G. 3 | 9.3, p. 656 |
| 9.3: Finding <br> Arc Lengths of Curves Given by Parametric Equations BC ONLY | CHA-6: Definite integrals allow us to solve problems involving the accumulation of change in length over an interval. <br> CHA-6.B: Determine the length of a curve in the plane defined by parametric functions, using a definite integral. BC ONLY | CHA-6.B. 1 | 9.3, pp. 657-658 |
| 9.4: Defining and Differentiating Vector-Valued Functions BC ONLY | CHA-3: Derivatives allow us to solve real-world problems involving rates of change. <br> CHA-3.H: Calculate derivatives of vector-valued functions. BC ONLY | CHA-3.H. 1 | 9.7, pp. 689-693 |
| 9.5: Integrating <br> Vector-Valued <br> Functions <br> BC ONLY | FUN-8: Solving an initial value problem allows us to determine an expression for the position of a particle moving in the plane. <br> FUN-8.A: Determine a particular solution given a rate vector and initial conditions. BC ONLY | FUN-8.A. 1 | 9.7, p. 694 |
| 9.6: Solving Motion Problems Using Parametric | FUN-8: Solving an initial value problem allows us to determine an expression for the position of a particle moving in the plane. <br> FUN-8.B: Determine values for positions and rates of change in problems involving planar motion. BC ONLY | FUN-8.B. 1 | 9.8, pp. 698-700 |
| Functions BC ONLY |  | FUN-8.B. 2 | 9.8, p. 701 |
| 9.7: Defining <br> Polar Coordinates | FUN-3: Recognizing opportunities to apply derivative rules can simplify differentiation. <br> FUN-3.G: Calculate derivatives of functions written in polar coordinates. BC ONLY | FUN-3.G. 1 | 9.4, pp. 663-669 |
| in Polar Form BC ONLY |  | FUN-3.G. 2 | 9.4, pp. 667-668 |


| Topic | Enduring Understanding and Learning Objective | Essential <br> Knowledge |  <br> Page Number(s) |
| :--- | :--- | :--- | :--- |
| 9.8: Finding the <br> Area of a Polar <br> Region or the Area <br> Bounded by a <br> Single Polar Curve <br> BC ONLY | CHA-5: Definite integrals allow us to solve problems involving the <br> accumulation of change in area or volume over an interval. | CHA-5.D: Calculate areas of regions defined by polar curves using <br> definite integrals. BC ONLY | CHA-5.D.1 | 9.5, pp. 673-674

Course: AP ${ }^{\circledR}$ Calculus BC Only
Unit 10: Infinite Sequences and Series
Suggested Length: AB Not Applicable BC ~17-18 class periods

AP Exam Weighting: AB Not Applicable BC 17-18\%

Big Ideas: Limits (LIM)
$\begin{array}{|l|l|l|l|}\hline \text { Topic }\end{array}$ Enduring Understanding and Learning Objective $\left.\begin{array}{l}\text { Essential } \\ \text { Knowledge }\end{array} \begin{array}{l}\text { Text Section(s) \& } \\ \text { Page Number(s) }\end{array}\right]$

Highlighting indicates topics and sections that are BC only.

| Topic | Enduring Understanding and Learning Objective | Essential <br> Knowledge |  <br> Page Number(s) |
| :--- | :--- | :--- | :--- |
| 10.7: Alternating <br> Series Test for <br> Convergence <br> BC ONLY | LIM-7: Applying limits may allow us to determine the finite sum of <br> infinitely many terms. <br> LIM-7.A: Determine whether a series converges or diverges. BC ONLY | LIM-7.A.10 | 8.5, pp. 569-574 |


| Topic | Enduring Understanding and Learning Objective | Essential Knowledge | Text Section(s) \& Page Number(s) |
| :---: | :---: | :---: | :---: |
| 10.13: Radius and Interval of Convergence of Power Series BC ONLY | LIM-8: Power series allow us to represent associated functions on an appropriate interval. <br> LIM-8.D: Determine the radius of convergence and interval of convergence for a power series. BC ONLY | LIM-8.D. 1 | 8.8, p. 597 |
|  |  | LIM-8.D. 2 | 8.8, pp. 598-599 |
|  |  | LIM-8.D. 3 | 8.8, p. 599 |
|  |  | LIM-8.D. 4 | 8.8, pp. 600-601 |
|  |  | LIM-8.D. 5 | 8.10, pp. 614-615 |
|  |  | LIM-8.D. 6 | 8.8, pp. 602-603 |
| 10.14: Finding <br> Taylor or <br> Maclaurin Series <br> for a Function <br> BC ONLY | LIM-8: Power series allow us to represent associated functions on an appropriate interval. <br> LIM-8.E: Represent a function as a Taylor series or a Maclaurin series. BC ONLY | LIM-8.E. 1 | 8.10, pp. 614-616 |
|  | LIM-8: Power series allow us to represent associated functions on an appropriate interval. <br> LIM-8.F: Interpret Taylor series and Maclaurin series. BC ONLY | LIM-8.F. 1 | 8.9, p. 607 |
|  |  | LIM-8.F. 2 | 8.10, pp. 617-622 |
| 10.15: <br> Representing <br> Functions as <br> Power Series <br> BC ONLY | LIM-8: Power series allow us to represent associated functions on an appropriate interval. <br> LIM-8.G: Represent a given function as a power series. BC ONLY | LIM-8.G. 1 | 8.9, pp. 607-611 |

